

# KALYAN ACADEMY

BHARATH NAGAR, HYD-18

REAL NUMBERS | CLASS X | WORKSHEET-2

- Write the following using logarithms instead of powers
  - $8^2 = 64$
  - $3^5 = 243$
  - $10^3 = 0.001$
  - $3^{-2} = 1/9$
  - $\sqrt{49} = 7$
  - $27^{2/3} = 9$
  - $32^{-2/5} = 1/4$
- Determine the value of the following logarithms
  - $\log_4 64$
  - $\log_{1/8} 8$
  - $\log_b 4\sqrt{b^3}$
  - $\log_{10} 0.001$
- Each of the following expressions can be simplified to  $\log N$ . Determine the value of  $N$  in each case. We have not explicitly written down the base. You can assume the base is 10, but the results are identical whichever base is used
  - $\log 12 - 2 \log 2 + \log 3$
  - $5 \log 2 + 4 \log 3 - 3 \log 4$
  - $\log 10 + 2 \log 3 - \log 2$
- Use the law of logarithms to expand the followings
  - $\log^3 \sqrt{x} \sqrt{y} / z$
  - $\log 5x^3y / 4$
  - $\log \sqrt{3x-5} / 7$
  - $\log_3^{9/mn}$
- Use Euclid division lemma to show that cube of any positive integer is either of the form  $9m$ ,  $9m + 1$ , or  $9m + 8$ ?
- Show that any positive odd integer is of the form  $6q + 1$ , or  $6q + 3$ , or  $6q + 5$ , where  $q$  is some integer?
- Use Euclid's algorithm to find the HCF of a) 4052 and 12576 b) 86 and 255 c) 196 and 38220
- Prove that square of any positive integer is of the form  $3m$  or  $3m+1$  for some integer?
- If the HCF of 210 and 55 is expressible in the form  $210x + 55y$ , Find  $y$ ?
- Prove that one of every three consecutive integers is divisible by 3?