

# KALYAN ACADEMY

BHARATH NAGAR, HYD-18

REAL NUMBERS | CLASS X | WORK SHEET-1

1. Show that any positive integer is of the form  $3q$  or  $3q+1$  or  $3q+2$  for some integer  $q$ ?
2. Show that  $n^2 - 1$  is divisible by 8, if  $n$  is an odd positive integer?
3. Show that the square of any positive integer is of the form  $3m$  or  $3m+1$  for some integer  $m$ ?
4. Use Euclid's division lemma to show that the cube of any positive integer is either of the form  $9m$  or  $9m+1$  or  $9m+8$  for some integer  $m$ ?
5. Show that the square of any positive integer is of the form  $5q$  or  $5q+1$  or  $5q+4$  for some integer  $q$ ?
6. Use Euclid's division algorithm to find HCF of the followings
  - a) 135 and 225
  - b) 210 and 55
  - c) 867 and 1155
7. Express the followings as a product of its prime factors
  - a) 468
  - b) 945
  - c) 420
8. Explain why  $7 \times 11 \times 13 + 13$  and  $7 \times 6 \times 5 \times 4 \times 3 \times 2 \times 1 + 5$  are composite numbers?
9. Check whether  $6^n$  can end with the digit 0 for any natural number  $n$ ?
10. Find the LCM and HCF of the following numbers by prime factorization method
  - a) 12, 15, 21
  - b) 24, 15, 36
  - c) 17, 23, 29
  - d) 8, 9, 25
11. Find HCF of 96 and 404 by prime factorization method. Hence find their LCM?
12. Prove the followings are irrational numbers
  - a)  $\sqrt{2}$
  - b)  $\sqrt{3}$
  - c)  $3\sqrt{2}$
  - d)  $5-\sqrt{3}$
  - e)  $\sqrt{2} + \sqrt{5}$
  - f)  $4 - 5\sqrt{2}$
13. Let  $a, b, c, d$  be positive rationals such that  $a + \sqrt{b} = c + \sqrt{d}$ , then either  $a=c$  and  $b=d$  or  $b$  and  $d$  are square of rationals.
14. Without actually performing the long division, state whether the followings are terminating, non terminating decimal expansions
  - a)  $23/8$
  - b)  $35/50$
  - c)  $77/210$
  - d)  $13/3125$
  - e)  $29/343$
  - f)  $15/1600$
15. Write down the decimal expansions of the following rational numbers by writing their denominators in the form of  $2^m \times 5^n$ , where  $m$  and  $n$  are non negative integers
  - a)  $13/125$
  - b)  $129/2^2 \times 5^7$
  - c)  $49/500$
16. Write down the following fractions denominators in the form of  $2^m \times 5^n$ 
  - a) 1.512
  - b) 0.01764
  - c) 0.875
  - d) 27.7624